# The braids Package: Documentation 

Andrew Stacey<br>stacey@math.ntnu.no<br>v1.0 from 2011/05/07



## 1 Introduction

This is a package for drawing braid diagrams using PGF/TikZ. An example follows.

```
\begin{center}
\begin{tikzpicture}
\braid [rotate = 90, style strands={1}{red}, style
    strands}={2}{\mathrm{ blue }, style strands}={3}{\mathrm{ green }] s__1
    s__2^{-1} s__ s__ 2^{-1} s__ s s__ 2^{-1};
\end{tikzpicture}
\end{center}
```



## 2 Usage

\braid A braid is specified by the command \braid. The syntax for this command is as follows:
\braid[style options] (name) at (coordinate) braid-word;
braid-word
The braid-word is an expression in the braid group, such as s_1 s_2^\{-1\}. The generator labels are not significant. The exponent can be $1,\{-1\}$, or missing (in which case it defaults to 1 , note also that the exponent is read as a $T_{E} X$-token so $\{1\}$ is also legal). Certain other symbols are allowed in the braid-word which control the rendering of the braid. To get crossings to render at the same height, separate them with a hyphen (note: no check is made to ensure that the crossings can legally be put at the same height; caveat emptor). To draw a floor, precede the braid element by a vertical line. What happens then is that when the braid is rendered, the coordinates of the rectangle behind that crossing (wide enough to encompass all the strands) is passed to a command. The intention is that this command draw something behind the braid. The command is configurable by a key (see 2.1). that set the default style for the strands, and options that set up styles for individual strands. The options are as follows.

### 2.1 Style Options

number of strands
The key number of strands sets the minimum number of strands for the braid The number of strands will grow according to the terms in the braid word so this merely sets a lower bound. If not set, the number of strands will be determined by the terms in the braid word.
height The key height sets the height of the piece of the braid corresponding to an element in the group.

The key width sets the separation of the strands in the braid.
The key border height adds a little extra length to the strands at the start
and end of the braid.
style strands
style of the strands are controlled by two types of option. Style options that are set on the \braid command are passed to every strand. It is also possible to add style options to individual strands using the key style strands. This takes two options, a comma-delimited list of strand numbers (which could be just a single number) and a list of options to be applied to that strand. Thus, the syntax is style strands $=\{n, m, \ldots\}\{o p t i o n s\}$. The strands are numbered by their starting position. Not all of the standard TikZ style options are possible due to the way that the strands are constructed. Basically, the options that are allowed are those that do not require changing the path or drawing it more than once.

When a floor is requested behind a crossing, the actual way to render it is determined by a command. This key allows the user to define that command. The argument to this key should be the code that should be executed for each floor. To avoid the hassle of getting the number of hashes right, the command should take no arguments. Rather, the coordinates of the rectangle are saved in to macros \floorsx, \floorsy, \floorex, \floorey (these macros will expand to something like 10 pt ) and the command should use these to position the drawing. The default is to draw a line at the top and at the bottom of the rectangle.
style floors
style all floors
In the spirit of separating style and content, the style options for the floors can be specified separately to the command (of course, they could be built in to the command). One advantage of this over building them in to the command is to allow them to be overridden for individual floors. The style all floors sets up options to be used for all floors, whilst the style floors $=\{n, m, \ldots\}\{o p t i o n s\}$ sets up options to be used only for the listed floor. Anything specified in the floor command will take precedence over both of these.

Any other style options are passed to the underlying TikZ/PGF system and so may influence how the braid is drawn (but note that not all keys make sense due to the implementation).

## 3 Example

Here is a more detailed example.

```
\begin{center}
\begin{tikzpicture}
\ \text { braid [}
    style all floors={fill=yellow },
    style floors={1}{dashed, fill=yellow!50!green},
    floor command={%
        \fill (\floorsx,\floorsy) rectangle
            (\ floorex,\ floorey);
        \draw (\floorsx,\floorsy) -- (\floorex ,\floorsy);
    },
    line width=2pt,
    style strands={1}{red},
    style strands={2}{blue},
    style strands={3}{green}
] (braid) at (2,0) | s__1-s_3-s_5 | s__2^{-1}-s__4| s__1-s_4
        s_2^{-1} s_1-s_3 s_2^{-1}-s__4^{-1};
\fill[yellow] (2,0) circle (4pt);
\fill[purple] (braid) circle (4 pt);
\node[at=(braid-3-s), pin=north west:strand 3] {};
\node[at=(braid-3-e), pin=south west:strand 3] {};
\node[at=(braid-rev-3-s), pin=north east:strand 3 (from
    bottom)] {};
\node[at=(braid-rev-3-e), pin=south east:strand 3 (from
        bottom)] {};
\end{tikzpicture}
\end{center}
```



